# ON A CONJECTURE OF ZIMMERMAN ABOUT AUTOMORPHISMS OF $S_{n}$ 

$$
\begin{aligned}
& \qquad \text { Abstract } \\
& \qquad \text { All groups considered are finte. For a group } G \text { and } \alpha \in \operatorname{Aut}(G) \text {, we set } \\
& \qquad S(G, \alpha)=\left\{g \in G \mid g \alpha=g^{2}\right\} \\
& \text { We let } s(G, \alpha)=\frac{|S(G, \alpha)|}{|G|} \text { and define the function } s(G) \text { by } s(G)=\max _{\alpha \in \operatorname{Aut}(G)} s(G, \alpha) \\
& \text { we calculate for the permutation group } S_{n} \text {. }
\end{aligned}
$$

