

Abstract

In the paper the upper estimations of smoothness L_r -module $\omega_m(h; \delta)_r$ of order m of the convolution $h = f * g$ of two 2π periodic functions $f \in L_p(\mathbb{T})$ and $g \in L_q(\mathbb{T})$ are obtained by means of the product expression $\omega_l(f; \delta)_p \omega_k(g; \delta)_q$ of smoothness modules of these functions, where $m, l, k \in \mathbb{N}$, $p, q \in [1, \infty]$, $1/r = 1/p + 1/q - 1 \geq 0$, $\mathbb{T} = (-\pi, \pi]$. In particular, it is proved in the case $p, q \in (1, \infty)$ that the obtained estimations are exact in the terms of order on classes of convolutions with given majorants of smoothness modules of f and g under some regularity of the majorants in the case $m < l + k$ and under arbitrary majorants in the case $m \geq l + k$.