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TO THE M.RIESZ THEOREM ON ABSOLUTE CONVERGENCE OF THE TRIGONOMETRIC FOURIER SERIES (THE SECOND REPORT)

Abstract

This paper is a continuation of the author's investigations in the same name paper on the extension of the known M.Riesz criterion for absolute convergence of trigonometric Fourier series of continuous functions for values $p \neq 2$. The case of functions $f \in L_p(T)$, $g \in L_q(T)$ generating the convolution h = f * gare considered, where 1 < p, q < 2. The exact upper estimate of $l^{r'}$ norm of sequence of Fourier coefficients of the convolution by product of norms $||f||_p \cdot ||g||_q$, where $r' = pq/(2pq - p - q) \in [1, \infty)$, as well as the upper estimate of residual series generating above mentioned lr' norm by product of the best (in metrics $L_p(T)$ and $L_q(T)$, respectively) approximations $E_{n-1}(f)_{\rho} \cdot E_{n-1}(g)_q$, $n \in \mathbb{N}$, of these functions are obtained, and its exactness in the sence of the order in the scale of power majorants was proved.